Infinity structures in rational homotopy theory

I will give a general introduction to rational homotopy theory, explain the role that higher homotopy algebras of type A-, C- and L-infinity play there, and sketch a Milnor-Moore theorem for L-infinity algebras.