Black holes as a mathematical problem

After an introduction to various aspects of black holes theory, I will describe current progress concerning the mathematics of black holes, and present open problems