

## Weiterführende Fragen der Ökonometrie

### Übungsaufgaben – Blatt 8

#### Aufgabe 1 (3 Punkte)

Consider the simple regression model

$$y = \beta_0 + \beta_1 x + u$$

and let  $z$  be a *binary* instrumental variable for  $x$ . Use (15.10) to show that the IV estimator  $\hat{\beta}_1$  can be written as

$$\hat{\beta}_1 = (\bar{y}_1 - \bar{y}_0) / (\bar{x}_1 - \bar{x}_0),$$

where  $\bar{y}_0$  and  $\bar{x}_0$  are the sample averages of  $y_i$  and  $x_i$  over the part of the sample with  $z_i = 0$ , and where  $\bar{y}_1$  and  $\bar{x}_1$  are the sample averages of  $y_i$  and  $x_i$  over the part of the sample with  $z_i = 1$ . This estimator, known as a *grouping estimator*, was first suggested by Wald (1940).

Quelle: Wooldridge 3e & 4e Problem 15.3

#### Aufgabe 2

Suppose that, for a given state in the United States, you wish to use annual time series data to estimate the effect of the state-level minimum wage on the employment of those 18 to 25 years old ( $EMP$ ). A simple model is

$$gEMP_t = \beta_0 + \beta_1 gMIN_t + \beta_2 gPOP_t + \beta_3 gGSP_t + \beta_4 gGDP_t + u_t,$$

where  $MIN_t$  is the minimum wage, in real dollars,  $POP_t$  is the population from 18 to 25 years old,  $GSP_t$  is gross state product, and  $GDP_t$  is U.S. gross domestic product. The  $g$  prefix indicates the growth rate from year  $t - 1$  to year  $t$ , which would typically be approximated by the difference in the logs.

- (i) (1 Punkt) If we are worried that the state chooses its minimum wage partly based on unobserved (to us) factors that affect youth employment, what is the problem with OLS estimation?
- (ii) (2 Punkte) Let  $USMIN_t$  be the U.S. minimum wage, which is also measured in real terms. Do you think  $gUSMIN_t$  is uncorrelated with  $u_t$ ?
- (iii) (2 Punkte) By law, any state's minimum wage must be at least as large as the U.S. minimum. Explain why this makes  $gUSMIN_t$  a potential IV candidate for  $gMIN_t$ .

Quelle: Wooldridge 3e & 4e Problem 15.4

### Aufgabe 3

- (i) (2 Punkte) In the model with one endogenous explanatory variable, one exogenous explanatory variable, and one extra explanatory variable, take the reduced form  $y_2 = \pi_0 + \pi_1 z_1 + \pi_2 z_2 + \nu_2$  (15.26), and plug it into the structural equation  $y_1 = \beta_0 + \beta_1 y_2 + \beta_2 z_1 + u_1$  (15.22). This gives the reduced form for  $y_1$ :

$$y_1 = \alpha_0 + \alpha_1 z_1 + \alpha_2 z_2 + \nu_1.$$

Find the  $\alpha_j$  in terms of the  $\beta_j$  and the  $\pi_j$ .

- (ii) (1 Punkt) Find the reduced form error,  $\nu_1$ , in terms of  $u_1$ ,  $\nu_2$ , and the parameters.
- (iii) (3 Punkte) How would you consistently estimate the  $\alpha_j$ ?

Quelle: Wooldridge 3e & 4e Problem 15.6

### Aufgabe 4

In Example 15.2 in Wooldridge (2009) the authors use the data in `wage2.txt` to estimate effect of education on the logarithm of wages for men. However, they use the variable *sibs* (number of siblings) as an instrument for *educ*.

- (i) (2 Punkte) In the regression with *sibs* as an instrument for *educ*, the IV estimate of the return to education is .122. To convince yourself that using *sibs* as an IV for *educ* is *not* the same as just plugging *sibs* in for *educ* and running an OLS regression, run the regression of  $\log(\text{wage})$  on *sibs* and explain your findings.
- (ii) (2 Punkte) The variable *brthord* is birth order (*brthord* is one for a first-born child, two for a second-born child, and so on). Explain why *educ* and *brthord* might be negatively correlated. Regress *educ* on *brthord* to determine whether there is a statistically significant negative correlation.
- (iii) (2 Punkte) Use *brthord* as an IV for *educ* in equation (15.1). Report and interpret the results.
- (iv) (3 Punkte) Now, suppose that we include number of siblings as an explanatory variable in the wage equation; this controls for family background, to some extent:

$$\log(\text{wage}) = \beta_0 + \beta_1 \text{educ} + \beta_2 \text{sibs} + u.$$

Suppose that we want to use *brthord* as an IV for *educ*, assuming that *sibs* is exogenous. The reduced form for *educ* is

$$\text{educ} = \pi_0 + \pi_1 \text{sibs} + \pi_2 \text{brthord} + \nu.$$

State and test the identification assumption.

- (v) (1 Punkt) Estimate the equation from part (iv) using *brthord* as an IV for *educ* (and *sibs* as its own IV). Comment on the standard errors for  $\hat{\beta}_{\text{educ}}$  and  $\hat{\beta}_{\text{sibs}}$ .

(vi) (2 Punkte) Using the fitted values from part (iv),  $\widehat{educ}$ , compute the correlation between  $\widehat{educ}$  and  $sibs$ . Use this result to explain your findings from part (v).

Quelle: Wooldridge 3e & 4e Computer Exercise C15.1